

1. Solve:

(a) $e^{x^2+y} dx + \frac{y}{2x} dy = 0$

(b) $xy^3 \frac{dy}{dx} = 1 - x^2 + y^2 - x^2y^2$

(c) $x^2(y+1) dx + y^2(x-1) dy = 0$

2. Solve:

(a) $[\cos x \tan y + \cos(x+y)] dx + [\sin x \sec^2 y + \cos(x+y)] dy = 0$

(b) $(3x^2 + 4y) dx + (4x - y + 1) dy = 0$

(c) $\frac{dy}{dx} = \frac{y+1}{(y+2)e^{y-x}}$

3. Solve:

(a) $(x^2 + y^2 + 2x) dx + 2y dy = 0$

(b) $(3x^2y^4 + 2xy) dx + (2x^3y^3 - x^2) dy = 0$

4. Solve:

(a) $y' + \frac{y}{x} = 4(1+x^2)$

(b) $y' + x \sin 2y = x^3 \cos^2 y$

(c) $(x + 2y^3) y' = y$

(d) $\left(xy - \frac{dy}{dx}\right) e^{x^2} = y^3$

5. Find general solutions for each of the following equations.

(a) $y'' + y' - 6y = 0$

(b) $y'' - 4y' + 4y = 0$

(c) $y'' - 4y = 0$

(d) $y'' - 5y' = 0$

6. Use the method of undetermined coefficients to solve each of the following:

(a) $y'' + y = x^2 + 2x$

(b) $y'' + 10y' + 25y = 20e^{-5x}$

(c) $y'' + y = x \sin x$

7. Use the method of variation of parameters to find solutions for each of the following:

(a) $y'' + 4y = \tan 2x$

(b) $y'' + 4y' + 5y = e^{-2x} \sec x$

(c) $y'' + y = \frac{1}{1+\sin x}$