Hybrid MOM-Immittance Approach for Full-Wave Characterization of Printed Strips and Slots in Layered Waveguide and Its Applications

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1. Introduction

Printed strips and slots are basic building blocks for many waveguide-based structures and they are printed on a dielectric layer. Commonly used waveguide elements like inductive and capacitive strips, diaphragms, iris, etc. [1]–[4] are special cases of printed strips and slots where the thickness of the dielectric layer is reduced to zero. An excellent literature on waveguide filters, impedance matching and coupling structures is given in [5] and equivalent circuits of many common waveguide elements are listed in [6], [7] using variational techniques. It is our objective to extract the equivalent circuits of printed strips and slots in layered waveguide using method-of-moments (MoM) so that cascaded network based synthesis design using such structures can be implemented easily. Planar strips and slots also have been studied for spatial power combining applications in [8].

In this paper, the admittance-type and impedance-type MoM are formulated respectively for printed slot and strip. The admittance approach as described in [9], [10] has been used to calculate spectral dyadic Green’s functions for arbitrary shape in layered waveguide for various applications has been proposed. An impedance-type MoM is formulated from the electric field integral equation (EFIE) for printed strip case and an admittance-type MoM is formulated from the magnetic field integral equation (MFIE) for the printed slot case, using the Galerkin’s technique. Immittance approach has been used to calculate spectral dyadic Green’s functions for the layered waveguide. For efficient analysis of large and complex structures, equivalent circuit parameters of a block are first extracted and complete structure is analyzed through cascaded ABCD matrices. The equivalent circuit characterization of printed strip and slot in layered waveguide has been done for the first time. Finite periodic structure loaded with printed strips has been investigated and it shows the electromagnetic bandgap (EBG) behavior. The electromagnetic (EM) program hence developed is checked for its numerical accuracy and efficiency with results generated with High-frequency structure simulator (HFSS) and shows good performance.

**key words:** printed strips and slots, method of moments, equivalent circuits, bandpass filter, periodic structures

2. Theoretical Formulation

2.1 Impedance-Type MoM Formulation

Figure 1 depicts the three-dimensional geometry of waveguide discontinuity under consideration. The layered waveguide can be divided into three regions, region I of relative permittivity \(\epsilon_1\), region II of relative permittivity \(\epsilon_2\) and region III of relative permittivity \(\epsilon_3\). The printed strip of any arbitrary shape and size is located at the interface #1. The thickness of the dielectric substrate layer i.e. region II is denoted by \(h\). The electromagnetic waves incident from region I are scattered at the interface #1 and transmitted through region II to region III. The electric field integral equation (EFIE) can be obtained from the boundary condition on the tangential components of the total electric field, which consists of incident and scattered electric field, on the printed strip is zero.

\[
\mathbf{n} \times \mathbf{E}^i(r) + \mathbf{n} \times \int_{\text{strip}} \mathbf{G}_{EJ}(r', r) \cdot \mathbf{J}(r') dS' = 0
\]

In the above equation, the scattered electric field is expressed in terms of electric dyadic Green’s functions and the multilayered waveguide structures with printed strips and/or printed slots. The electromagnetic (EM) program hence developed has been checked for its accuracy for various waveguide elements with the High-frequency structure simulator (HFSS) results and shows good agreement. Then, equivalent circuit parameters of printed strip and slot in layered waveguide have been extracted. Finite periodic structure loaded with printed strip has also been investigated. Finally a compact and broadband band pass filter has been designed using our proposed method and compared with HFSS.

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**Fig. 1** Geometry of printed strip in layered waveguide.

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**SUMMARY** A hybrid method-of-moments (MoM) and imittance approach for efficient and accurate analysis of printed slots and strips of arbitrary shape in layered waveguide for various applications has been proposed. An impedance-type MoM is formulated from the electric field integral equation (EFIE) for printed strip case and an admittance-type MoM is formulated from the magnetic field integral equation (MFIE) for the printed slot case, using the Galerkin’s technique. Immittance approach has been used to calculate spectral dyadic Green’s functions for the layered waveguide. For efficient analysis of large and complex structures, equivalent circuit parameters of a block are first extracted and complete structure is analyzed through cascaded ABCD matrices. The equivalent circuit characterization of printed strip and slot in layered waveguide has been done for the first time. Finite periodic structure loaded with printed strips has been investigated and it shows the electromagnetic bandgap (EBG) behavior. The electromagnetic (EM) program hence developed is checked for its numerical accuracy and efficiency with results generated with High-frequency structure simulator (HFSS) and shows good performance.

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electric current density over the printed strip. After discretizing the electric current density over the strip by using appropriate basis functions and applying Galerkin’s method, we can transform the EFIE into matrix systems of linear equations. Using Fourier transform technique and after doing some mathematical manipulations, we have arrived at a simple expression for impedance-type MoM matrix equation.

where the elements of each sub-matrices are expressed as

\[
\begin{bmatrix}
Z_{xx} & Z_{xy} \\
Z_{yx} & Z_{yy}
\end{bmatrix}
\begin{bmatrix}
I_x \\
I_y
\end{bmatrix}
= \begin{bmatrix}
V_x \\
V_y
\end{bmatrix}
\quad (2)
\]

In the above equation, \(B_x(x,y), B_y(x,y)\) are the \(x\)- and \(y\)-directed basis functions while \(T_x(x,y), T_y(x,y)\) are the \(x\)- and \(y\)-directed testing functions. In Galerkin’s method, basis functions are chosen the same as the testing functions which is composed of piecewise sinusoidal functions along current direction and pulse functions in the transverse direction. \(\tilde{B}_x(x,y), \tilde{B}_y(x,y)\) are the Fourier transform pairs of \(x\)- and \(y\)-directed basis functions while \(\tilde{T}_x(x,y), \tilde{T}_y(x,y)\) are the complex conjugate of the Fourier transform pairs of \(x\)- and \(y\)-directed testing functions. The sub-matrices \([V_x]\) and \([V_y]\) refer to the \(x\)- and \(y\)-directed testing of the incident electric field. We have considered the case for the dominant \(TE_{10}\) mode only here. By choosing incident mode for other higher modes, we can also do the multimode full-wave analysis of such kinds of structures. \([I_x]\) and \([I_y]\) sub-matrices are the respective unknown electric current expansion coefficients associated with \(x\)-directed and \(y\)-directed basis functions. For the printed strip inside layered waveguide of geometry shown in Fig. 1, the equivalent transverse electric (TE) and transverse magnetic (TM) transmission line model [9], [10] using the immittance approach is as shown in Fig. 2.

In Fig. 2, \(Z_{TE}^E, Z_{TM}^E\) and \(Z_{TE}^T\) are respectively the wave impedances of TE mode in region I, region II, and region III of the waveguide. Similarly, \(Z_{TM}^E, Z_{TM}^T\) and \(Z_{TM}^T\) are respectively the wave impedances of TM mode in region I, region II, and region III of the waveguide. The equivalent impedance looking up from the interface #1 for the TE and TM mode cases are

\[
\begin{align*}
Z_{TE}^E &= Z_{11}^E, \quad Z_{TM}^E = Z_{11}^T \\
\end{align*}
\]

Whereas the equivalent impedance looking down from the interface #1 for the TE and TM mode cases are

\[
\begin{align*}
Z_{TE}^E &= Z_{33}^E/Z_{32}^E + jZ_{33}^T/Z_{32}^T \tanh(\gamma_z h) \\
Z_{TM}^E &= Z_{33}^T/Z_{32}^T + jZ_{33}^T/Z_{32}^T \tanh(\gamma_z h) \\
\end{align*}
\]

In the above equation, \(\gamma_z\) is the propagation constant of EM wave in the waveguide region II. Let us denote the equivalent impedance by \(Z_{TE}\) for TE mode then \(Z_{TE} = Z_{TE}^E \parallel Z_{TE}^T\) due to the shunt combination of \(Z_{TE}^E\) and \(Z_{TE}^T\); similarly let us denote the equivalent impedance for TM mode by \(Z_{TM}\) then \(Z_{TM} = Z_{TM}^E \parallel Z_{TM}^T\). The electric dyadic Green’s function in the spectral domain when the source and observation points are both at the interface #1 is

\[
\tilde{G}^{(1)}_{E,j}(k_x, z = 0, z' = 0) = -V_{jE}^T(k_x, 0, 0)(\tilde{k}_x \times \tilde{z})(\tilde{k}_x \times \tilde{z}) \\
\tilde{V}_{jE}^T(k_x, 0, 0)(\tilde{k}_x)(\tilde{k}_x)
\]

The primed \(z\) coordinates represent the source locations whereas the unprimed \(z\) coordinates represent the observation point. \(V_{jE}^T\) and \(\tilde{V}_{jE}^T\) are the voltage across the interface #1 for TE and TM mode respectively. \(k_x\) is the transverse vector wave number and can be expressed as

\[
k_x = k_{x0}\hat{x} + k_{y0}\hat{y} = \left(\frac{m\pi}{a}\right)\hat{x} + \left(\frac{n\pi}{b}\right)\hat{y} = |k|\hat{k}
\]
\[
\begin{align*}
\tilde{G}^{zz}(k_i, z = h, z' = 0) &= -V_{TE}^2(k_i, h, 0)(\hat{k}_i \times \hat{z})(\hat{k}_i \times \hat{z}) \\
&= -\frac{Z_{TM}^2}{Z_{TE}^2} \left( \hat{k}_i \times \hat{z} \right)(\hat{k}_i \times \hat{z}) \\
&= -\left\{ Z_{TM}^2 \times \frac{Z_{TE}^2}{Z_{TM}^2} \right\} (\hat{k}_i \times \hat{z})(\hat{k}_i \times \hat{z})
\end{align*}
\]

In the above equation, \( V_{TE}^2 \) and \( V_{TM}^2 \) are the voltage across the interface \#2 for TE and TM mode respectively. The four components of the electric dyadic Green’s function in the spectral domain of Eqs. (5) and (7) can be obtained as

\[
\begin{align*}
\tilde{G}_{xx}(k_{xm}, k_{yn}) &= -\frac{k_{xm}^2 Z_{TM} + k_{yn}^2 Z_{TE}}{k_{xm}^2 + k_{yn}^2} \\
\tilde{G}_{yy}(k_{xm}, k_{yn}) &= -\frac{k_{xm}^2 Z_{TE} + k_{yn}^2 Z_{TM}}{k_{xm}^2 + k_{yn}^2} \\
\tilde{G}_{xy/yz}(k_{xm}, k_{yn}) &= -\frac{k_{xm} k_{yn}(Z_{TM} - Z_{TE})}{k_{xm}^2 + k_{yn}^2}
\end{align*}
\]

2.2 Admittance-Type MoM Formulation

Figure 3 shows the three-dimensional geometry of waveguide discontinuity under consideration. The printed slot of any arbitrary shape and size is located at the interface \#2. The magnetic field integral equation (MFIE) is obtained by enforcing boundary condition on the tangential components of the total magnetic field, which consists of incident and scattered magnetic field, on the printed slot is zero.

\[
\hat{z} \times H^{inc}(r_i) + \hat{z} \times \int_{\text{slot}} G_{HH}(r_i, r_s) \cdot M(r_s) dS_s = 0
\]

In the above equation, the scattered magnetic field is expressed in terms of magnetic dyadic Green’s functions and magnetic current density over the slot. After discretizing the magnetic current density over the slot by using appropriate basis functions and applying Galerkin’s method, we get the admittance-type MoM matrix equation as follows

\[
\begin{bmatrix}
Y_{xx} & Y_{xy} \\
Y_{yx} & Y_{yy}
\end{bmatrix}
\begin{bmatrix}
[V_x] \\
[V_y]
\end{bmatrix} =
\begin{bmatrix}
[I_x] \\
[I_y]
\end{bmatrix}
\]

where the elements of each sub-matrices are expressed as

\[
Y_{xx} = \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} B_x(k_{xm}, k_{yn}) \tilde{G}_{xx}^{TE}(k_{xm}, k_{yn}) T_x^+(k_{xm}, k_{yn}) + \tilde{G}_{xx}^{TM}(k_{xm}, k_{yn}) T_x^-(k_{xm}, k_{yn})
\]

\[
y_{xx}(m, n) = -\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} B_x(k_{xm}, k_{yn}) \tilde{G}_{xx}^{TM}(k_{xm}, k_{yn}) T_y^+(k_{xm}, k_{yn})
\]

\[
y_{xx}(m, n) = -\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} B_y(k_{xm}, k_{yn}) \tilde{G}_{yy}^{TE}(k_{xm}, k_{yn}) T_y^-(k_{xm}, k_{yn})
\]

\[
y_{yy}(m, n) = -\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} B_y(k_{xm}, k_{yn}) \tilde{G}_{yy}^{TM}(k_{xm}, k_{yn}) T_y^-(k_{xm}, k_{yn})
\]

\[
\begin{align*}
I_x &= \int_{\text{strip}} T_x^+(x, y) H_x^{inc}(x, y) dx dy \\
I_y &= \int_{\text{strip}} T_y^+(x, y) H_y^{inc}(x, y) dx dy
\end{align*}
\]

\[y_{TE}^{TM} = y_1^{TM}, \quad y_{TM}^{TM} = y_3^{TM}\]

Whereas the equivalent admittance looking up from the interface \#2 for the TE and TM mode cases are

![Fig. 4](https://via.placeholder.com/150)

**Fig. 4** Equivalent TE/TM transmission line model for transverse magnetic point source excitation in waveguide.
In the above equation, $\gamma_2$ is the propagation constant of EM wave in the waveguide II. The magnetic dyadic Green’s function in spectral domain when the source and observation points are both at the interface #2 is

$$G_{HM}^{22}(k_x, z, h, z' = h) = -i_d^T(k_x, h) (\hat{k}_x \times \hat{z})(\hat{k}_x \times \hat{z})$$

$$-i_d^M(k_x, h) (\hat{k}_x)(\hat{k}_x)$$

$$Y_{TE}^T(\hat{k}_x \times \hat{z})(\hat{k}_x \times \hat{z}) + Y_{TM}^T(\hat{k}_x)(\hat{k}_x)$$

Equation (13)

$I_a^T$ and $I_a^M$ denote the current flowing downward from the interface #2 for TE and TM mode respectively. Similarly, the magnetic dyadic Green’s function in spectral domain when the source is at the interface #1 and observation point is at the interface #1 is

$$G_{HM}^{11}(k_x, z, 0, z' = h) = -i_d^T(k_x, 0, h) (\hat{k}_x \times \hat{z})(\hat{k}_x \times \hat{z})$$

$$-i_d^M(k_x, 0, h) (\hat{k}_x)(\hat{k}_x)$$

$$Y_{TE}^T(\hat{k}_x \times \hat{z})(\hat{k}_x \times \hat{z}) - Y_{TM}^T(\hat{k}_x)(\hat{k}_x)$$

Equation (14)

$I_a^T$ and $I_a^M$ denote the current flowing upward from the interface #2 towards interface #1 for TE and TM mode respectively. The above method can be easily extended for any number of layers inside the waveguide and hence the MoM developed can be used for analysis of multiple numbers of printed strips and slots in multi-layered waveguide environment.

2.3 Equivalent Circuit Parameter Extraction

A reciprocal two-port network can be represented by either a T- or π-network as shown in Fig. 5. The elements of a two-port network can be calculated from the transmission matrix by a simple transformation as below:

$Z_n = (A - 1)/C$ \hspace{1cm} $Z_b = (D - 1)/C$ \hspace{1cm} $Z_c = 1/C$

$Y_n = (D - 1)/B$ \hspace{1cm} $Y_b = (A - 1)/B$ \hspace{1cm} $Y_c = 1/B$

The transmission matrix can be obtained from the scattering matrix as follows:

$$Y_n = \frac{Y_{TE}^2 + jY_{TE}^2 \tanh(\gamma_2 h)}{Y_{TE}^2 + jY_{TE}^2 \tanh(\gamma_2 h)}$$

$$Y_n = \frac{Y_{TM}^2 + jY_{TM}^2 \tanh(\gamma_2 h)}{Y_{TM}^2 + jY_{TM}^2 \tanh(\gamma_2 h)}$$

Equation (12)

$$A = ((1 + s_{11})(1 - s_{22}) + s_{12}s_{21})/2s_{21}$$

$$B = Z_0((1 + s_{11})(1 + s_{22}) - s_{12}s_{21})/2s_{21}$$

$$C = (1/Z_0)((1 - s_{11})(1 - s_{22}) - s_{12}s_{21})/2s_{21}$$

$$D = ((1 - s_{11})(1 + s_{22}) + s_{12}s_{21})/2s_{21}$$

Equation (16)

where $Z_0$ is the wave impedance of the dominant $TE_{10}$ mode. From the unitary condition of a lossless two-port junction, we have, $s_{22} = \frac{-Z_0}{Z_{12}}$ and for a reciprocal network $s_{12} = s_{21}$. Hence, only two parameters are independent for a reciprocal lossless two-port junction and they can be found by employing the following formulas:

$$s_{11} = E_{scattered}(r)/E_{incident}(r) \text{ at } z = 0^-, z' = 0^-$$

$$s_{12} = E_{scattered}(r)/E_{incident}(r) \text{ at } z = h^+, z' = 0^-$$

Equation (17)

For lossless networks, the impedance or admittance elements are purely imaginary. Hence, we can get the equivalent circuit parameters from the sign of the impedance or admittance elements.

3. Numerical Results

It has been observed that for obtaining convergent results the slot or strip surface must be divided into at least 10 numbers of meshes. For accurate scattering parameter results, the number of meshes should be chosen as 15 for the dimension of slot or strip equal to the free space wavelength at the frequency under consideration. Figures 6(a) and 6(b) illustrate the convergence plot of S-parameter amplitude and phase for a printed slot of dimension $w = 17$ mm and $l = 3$ mm placed inside a X-band rectangular waveguide ($a = 22.86$ mm and $b = 10.16$ mm) at 17 GHz. The three regions of the waveguide have $\epsilon_1 = 1.0$, $\epsilon_2 = 1.7$, $\epsilon_3 = 1.0$ and $h$ is taken as 1.0 mm. It can be seen that the amplitude of $s_{11}$ starts to converge around 10 numbers of meshes. For the phase of $s_{11}$ parameter the convergent result is obtained when the number of meshes is about 15.

3.1 Numerical Verifications

Let us consider the case of printed strip in a layered waveguide as shown in Fig. 7(a). A rectangular strip of $l = 9.0$ mm and $w = 3.0$ mm is placed at the center of an X-band rectangular waveguide. The three regions as illustrated in Fig. 1 have $\epsilon_1 = 1.0$, $\epsilon_2 = 2.25$, $\epsilon_3 = 1.0$ and $h$ is taken as 1.0 mm. The scattering parameters for a resonant printed strip inside an X-band rectangular waveguide is plotted using the developed EM program and shows good agreement with HFSS results as illustrated in Fig. 8. It has been observed that the printed strip totally reflects the incident wave at the resonance. Next, let us consider the case of printed slot in a layered waveguide as shown in Fig. 7(b). A rectangular slot of $l = 2.7$ mm and $w = 15.5$ mm is placed at the center of an X-band rectangular waveguide. The three regions have $\epsilon_1 = 1.0$, $\epsilon_2 = 2.25$, $\epsilon_3 = 1.0$ and $h$ is taken as 1.0 mm. The scattering parameters for a resonant printed
Fig. 6 Rate of convergence of a printed slot inside a rectangular waveguide (a) amplitude and (b) phase of $s_{11}$.

Fig. 7 Geometry of (a) printed rectangular strip (b) printed rectangular slot.

Fig. 8 Scattering parameter for a resonant printed strip in layered waveguide.

Fig. 9 Scattering parameter for a resonant printed slot in layered waveguide.

Fig. 10 (a) Equivalent circuit, (b) Normalized $X_a$ versus frequency and (c) Normalized $X_c$ versus frequency for resonant printed strip in layered waveguide.

A plot of the scattering parameter for a resonant printed slot inside an X-band rectangular waveguide is plotted using the developed EM program and shows good agreement with HFSS results as illustrated in Fig. 9. It has been observed that the printed slot totally transmits the incident wave at the resonance.
3.2 Equivalent Circuits

The equivalent circuit of printed strip is shown in Fig. 10(a) and its equivalent circuit parameters in layered waveguide have been extracted following the method described in Sect. 2.3. Figures 10(b) and 10(c) show the variation of normalized $X_b$ and $X_c$ with frequency in the equivalent T-network of Fig. 5(b) for various strip dimensions. From Fig. 10(b) we can infer that the normalized $X_b$ is positive and quasi-linearly increasing with frequency thereby it acts as an inductor. It can be observed from Fig. 10(c) that the normalized $X_c$ is negative at lower frequency region then crosses the zero axis and becomes positive at higher frequency region showing the series resonant behavior. It can be further observed that as we increase the length of the resonant printed strip, the resonant frequency is lowered. Normalized $X_b$ is very small and can be neglected in the equivalent T-network. The equivalent circuit of printed slot is shown in Fig. 11(a). Figures 11(b) and 11(c) show the variation of normalized $X_b$ and $X_c$ with frequency in the equivalent T-network for various slot dimensions. Normalized $X_b$ is positive and increases linearly with frequency as illustrated in Fig. 11(b) hence it acts as an inductor. From Fig. 10(c), we can infer that the normalized $X_c$ is positive in the lower frequency range then goes towards $+\infty$ and suddenly comes down to $-\infty$ around the resonant frequency and becomes negative at the higher frequency range which shows the parallel resonant behavior. We can also observe that the resonant frequency is lowered when the width of the slot is increased. Normalized $X_a$ is also very small and can be neglected in the equivalent T-network.

3.3 Finite Periodic Structures

A finite periodic waveguide structure loaded with units/cells of printed strips of $l = 9.0$ mm and $w = 3.0$ mm and thickness of dielectric layer $h = 1.0$ mm of period $p$ inside an X-
band waveguide has been investigated. The geometry and equivalent circuit topology of the unit cell is illustrated in Fig. 12(a). Figure 12(b) shows the insertion loss (dB) for finite periodic structure with number of unit cells $N = 3, 5$ and 7 for fixed period $p = 4.00$ mm. It can be observed that as the $N$ increases, the insertion loss goes into deep rejection band as mentioned in many literatures like [11]. For $N = 7$, the bandgap or bandstop as defined in [12] is 6.5 GHz for $s_{21}$ below $-30$ dB at the center frequency of 12.6 GHz which is a very wide bandstop. It has also been observed that there is frequency shift in the electromagnetic bandgap (EBG) as the period of the unit cell changes as illustrated in Fig. 12(c). As the period of unit cell is increased, the EBG of the finite periodic structure shifts to a lower frequency region for a fixed number of unit cells.

3.4 Band Pass Filter

Microwave filters are usually designed for size reduction and/or increased out-of-band rejection [13]. Let us consider a waveguide filter composed of resonant iris i.e. printed slot with no dielectric layer ($h = 0$). A compact and broadband iris filter has been designed based on the simple equivalent transmission line network, in which each parameter is derived using the proposed method. The geometry of the waveguide filter is shown in Fig. 13(a). The distance $d$ between resonant irises is taken as 9.0 mm. The dimension of the iris is $w = 15.5$ mm and $l = 2.7$ mm. The overall ABCD parameter of the filter is obtained by cascading ABCD parameters of every block and is transformed back to scattering parameters to observe the filter performance. The predicted result is compared with those of HFSS as shown in Fig. 13(b) and they are in good agreement. The waveguide filter shows the broadband characteristics with bandwidth = 28.0% for $s_{11}$ below $-15$ dB at the centre frequency of 10.7 GHz. It takes around 13hrs for the HFSS simulation. But the proposed method takes just several minutes to simulate a single iris then it takes just few seconds to get the performance of the overall filter. Hence the proposed method is more efficient than HFSS specially for designing high-order bandpass filters.

4. Conclusion

A hybrid MoM and immittance approach has been proposed for efficient and accurate analysis of printed strips and slots in layered waveguide. Equivalent circuit parameters are extracted for printed strips and slots in the layered waveguide so that cascaded network based synthesis design can be executed. The method developed is verified in comparison with the results obtained using HFSS and shows good agreement. The proposed MoM will be a very useful tool for various applications like filter design, waveguide synthesis design and full-wave analysis of finite periodic structures.

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References


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